

## EE213 Exam 2

April 23, 2014

Closed Book, Justify all work unless otherwise instructed.

Good Luck

NAME\_\_\_\_\_

student ID number \_\_\_\_\_

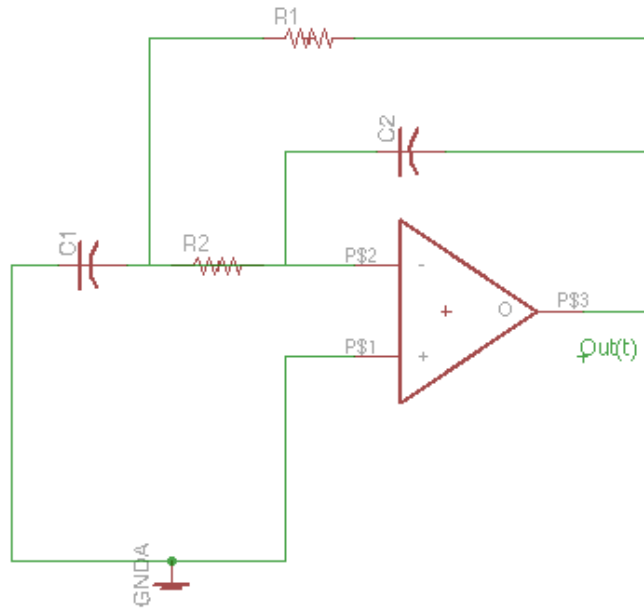
1	/25
2	/25
3	/30
4	/20
TOTAL	/100

1) (25) Consider the following system where the impulse response is given by  $h(t) = \exp(-2t)u(t)$  and the input is given by  $x(t) = \exp(-2t)(u(t) - u(t - 3))$ .

a) Use the convolution integral to compute the output  $y(t)$  by hand.

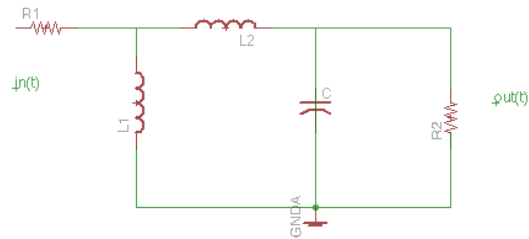
b) For the given impulse response above find the natural response.

2) (25) Consider the circuit below with no input and output voltage given by  $out(t)$ . Let the leftmost capacitor have an initial voltage  $v_{C_1}(0) = 2V$  and the rightmost capacitor have an initial voltage of  $v_{C_2}(0) = 1V$ . Both voltages are from left to right. Let  $C_1 = C_2 = 1F$ ,  $R_1 = 1\Omega$ , and  $R_2 = 0.5\Omega$ . Find the zero input response.



**3)** (30) Consider the circuit below with input voltage  $in(t)$  and output voltage  $out(t)$ . Here  $R_1 = R_2 = 1\Omega$ ,  $C = 1F$ ,  $L_1 = 1H$ , and  $L_2 = 0.5H$ .

- Determine the state of the system (find  $x(t)$ ) labeling direction of appropriate voltages and currents.
- Find the state space representation; A, b, c, d.
- Write MATLAB code to find the total response given the input is  $in(t) = \exp(-2t)u(t)$  and the initial voltage of the capacitor from top to bottom is  $v_C(0) = 1V$ , the initial current of the inductor from top to bottom is  $i_{L_1}(0) = 1A$ , and the initial current of the second inductor from left to right is  $i_{L_2}(0) = 1A$ .



4) (20) Consider the following four transfer functions. For each transfer function find all poles and all zeros. Then match each transfer function with one of the four plots of step responses.

$$H_1(s) = \frac{4s}{s^2 + 4s + 8}$$

$$H_2(s) = \frac{s^2}{s^2 + 4s + 4}$$

$$H_3(s) = \frac{8}{s^2 + 4s + 8}$$

$$H_4(s) = \frac{4}{s^2 + 4s + 4}$$

