# EE213 Exam 2 <br> April 23, 2014 

Closed Book, Justify all work unless otherwise instructed.

## Good Luck

## NAME

student ID number $\qquad$

| 1 | $/ 25$ |
| :---: | ---: |
| 2 | $/ 25$ |
| 3 | $/ 30$ |
| 4 | $/ 20$ |
| TOTAL | $/ 100$ |

1) (25) Consider the following system where the impulse response is given by $h(t)=\exp (-t) u(t)$ and the input is given by $x(t)=\exp (t)(u(t)-u(t-2))$.
a) Use the convolution integral to compute the output $y(t)$ by hand.
b) For the given impulse response above find the natural response.
2) (25) Consider the circuit below with no input and output voltage given by out $(t)$. Let the leftmost capacitor have an initial voltage $v_{C_{1}}(0)=1 V$ and the rightmost capacitor have an initial voltage of $v_{C_{2}}(0)=2 V$. Both voltages are from left to right. Let $C_{1}=C_{2}=1 F, R_{1}=1 \Omega$, and $R_{2}=1 \Omega$. Find the zero input response.

3) (30) Consider the circuit below with input voltage $i n(t)$ and output voltage out $(t)$. Here $R_{1}=$ $R_{2}=1 \Omega, C=1 F, L_{1}=1 H$, and $L_{2}=0.5 H$.
a) Determine the state of the system (find $x(t)$ ) labeling direction of appropriate voltages and currents.
b) Find the state space representation; A, b, c, d.
c) Write MATLAB code to find the total response given the input is $i n(t)=\exp (-2 t) u()$ and the initial voltage of the capacitor from top to bottom is $v_{C}(0)=1 V$, the initial current of the inductor from left to right is $i_{L_{1}}(0)=1 A$, and the initial current of the second inductor from top to bottom is $i_{L_{2}}(0)=1 \mathrm{~A}$.

4) (20) Consider the following four transfer functions. For each transfer function find all poles and all zeros. Then match each transfer function with one of the four plots of step responses.

$$
\begin{aligned}
& H_{1}(s)=\frac{5}{s^{2}+6 s+5} \\
& H_{2}(s)=\frac{s^{2}}{s^{2}+6 s+18} \\
& H_{3}(s)=\frac{6 s}{s^{2}+6 s+5} \\
& H_{4}(s)=\frac{6 s}{s^{2}+6 s+18}
\end{aligned}
$$




Mahanaloha



